

$M(2 \ 13)$

$(x \ y \ z)$

$(x \ y \ z)$

$(21 \ 3)$

$\theta \quad \theta \quad \text{---} \quad - \quad \theta$

A

$l_1: x \ my \ 1 \ 0 \quad l_2: mx \ 4y \ 2 \ 0$

$1u4 \ m^2 \ 0$

$m \ 2 \quad m \ 2$

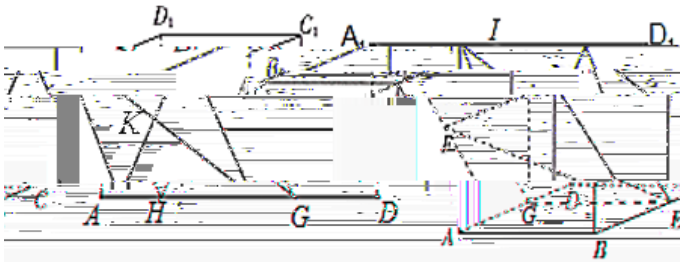
$m \ 2 \quad l_1: x \ 2y \ 1 \ 0 \quad l_2: 2x \ 4y \ 2 \ 0$

$m \ 2 \quad A$

A



$$\begin{aligned}
 & M(x_1, y_1) = k \cdot y - k(x - x_1) - y_1 = \frac{y - y_1}{x - x_1} \cdot k \cdot M(x_1, y_1) \\
 & x, y \quad a, b \quad \frac{x}{a} - \frac{y}{b} = 1 \\
 & b = 0 \quad y = kx - b - y \quad b \\
 & l: ax - y - 1 = 0 \quad AB \quad (f, \frac{3}{2}] \cup [2, \infty) \\
 & l \quad AB \quad a \cdot \frac{3}{2}
 \end{aligned}$$



$$\because BC = 2BB_1 = 6 \quad E \quad BC \quad C \quad AA_1 = 3 \quad AG = 4 \quad A_1G = 5$$

$$\therefore \cos \angle A_1GA = \frac{AG}{A_1G} = \frac{KG}{HG} \quad ? \quad HG = A_1I = \frac{25}{8}$$

$$F \quad I \quad H \quad A_1F \quad \frac{25}{8}$$

$$F \quad K \quad A_1F \quad \frac{5}{2}$$

$$A_1F \quad \frac{5}{2}, \frac{25}{8} \quad D \quad ACD$$

$$\vec{a} \quad \vec{a} = \vec{b} \quad \lambda$$

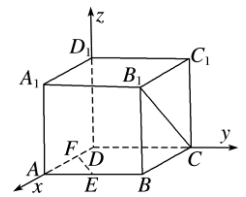
$$\lambda \quad \frac{1}{2x} \quad \frac{x}{8} \quad \frac{y}{5} \quad 0$$

$$l_1 A l_2 \quad (a \quad b) \quad 1 \quad 2b \quad 0 \quad a \quad 2b \quad 1 \quad a \quad 0, b \quad 0$$

$$\frac{2}{a} \quad \frac{1}{b} \quad \frac{2}{a} \quad \frac{1}{b} \quad (a \quad 2b) \quad \frac{2}{a} \quad \frac{2}{b} \quad \frac{4b}{a} \quad \frac{a}{b} \quad 4 \quad 2\sqrt{\frac{4b}{a} \frac{a}{b}} = 8$$

$$\frac{4b}{a} \quad \frac{a}{b} \quad a \quad \frac{1}{2}, b \quad \frac{1}{4} \quad \frac{2}{a} \quad \frac{1}{b}$$

$\sqrt{\quad}$



θ

$$\theta = \frac{2 \times \frac{2}{\sqrt{\quad}}}{\sqrt{\quad}} = \frac{2}{\sqrt{\quad}}$$

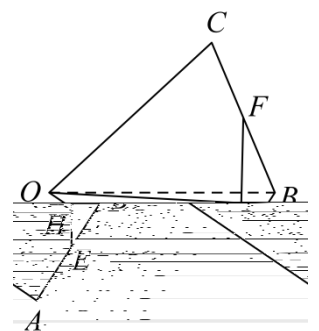
$$\theta = \frac{\sqrt{\quad}}{\sqrt{\quad}} = \frac{\sqrt{\quad}}{\sqrt{\quad}}$$

$$\frac{1}{3}, \frac{1}{2}, \frac{1}{6} \quad \frac{\sqrt{17}}{6}$$

E F

AB BC

$$\vec{OF} = \frac{1}{2} \vec{OB} + \vec{OC}$$



$$\overline{OE} \frac{1}{2} \overline{OA} \overline{OB} \quad \overline{EF} \frac{1}{2} \overline{OC} \frac{1}{2} \overline{OA} \quad H \quad EF \quad EH \frac{1}{3} EF \quad \overline{EH} \frac{1}{6} \overline{OC} \frac{1}{6} \overline{OA}$$

$$\overline{OH} \overline{OE} \overline{EH} \frac{1}{3} \overline{OA} \frac{1}{2} \overline{OB} \frac{1}{6} \overline{OC} \quad x, y, z \quad \frac{1}{3}, \frac{1}{2}, \frac{1}{6}$$

$$OAA \circ OB \quad \overline{OAA} \overline{OC} \quad |\overline{OA}| \quad |\overline{OB}| \quad |\overline{OC}| \quad 1$$

$$\overline{OA} \overline{OB} \sim 0 \quad \overline{OA} \overline{OC} \sim 0 \quad \overline{OB} \overline{OC} \sim \frac{1}{2} \quad \overline{OH} \frac{1}{3} \overline{OA} \frac{1}{2} \overline{OB} \frac{1}{6} \overline{OC}$$

$$|\overline{OH}| \sqrt{\frac{1}{9} \overline{OA}^2 + \frac{1}{4} \overline{OB}^2 + \frac{1}{36} \overline{OC}^2} \quad \sqrt{\frac{1}{9} \overline{OA}^2 + \frac{1}{4} \overline{OB}^2 + \frac{1}{36} \overline{OC}^2} \frac{1}{3} \overline{OA} \overline{OB} \frac{1}{9} \overline{OA} \overline{OC} \frac{1}{6} \overline{OB} \overline{OC}$$

$$\sqrt{\frac{1}{9} \frac{1}{4} \frac{1}{36} \frac{1}{12}} \quad \sqrt{\frac{17}{36}} \quad \frac{\sqrt{17}}{6} \quad \frac{1}{3}, \frac{1}{2}, \frac{1}{6} \quad \frac{\sqrt{17}}{6}$$

$C(m,n)$

$$QAB \quad CM \quad x \ y \ 3 \ 0 \ AC \quad BH \quad x \ 2y \ 2 \ 0$$

$$\begin{matrix} -m & n & 3 & 0 \\ \circledast n & 2 & \frac{1}{2} & \\ -m & 4 & 2 & \end{matrix} u \quad 1 \quad \begin{matrix} -m & 3 \\ \circledast -n & 0 \end{matrix} C(3,0)$$

$$B(a,b) \quad \begin{matrix} \circledast a & 2b & 2 & 0 \\ \circledast a & 4 & \frac{2}{2} & b \\ \circledast & 2 & \frac{2}{2} & 3 \end{matrix} \quad \begin{matrix} -a & \frac{10}{3} \\ b & \frac{2}{3} \end{matrix} \quad B \quad \frac{10}{3}, \frac{2}{3}$$

$$AC \quad 2x \ y \ 6 \ 0 \quad B \quad AC \quad d \quad \frac{2u \frac{10}{3} \ \frac{2}{3} \ 6}{\sqrt{2^2 + 1^2}} \quad \frac{4\sqrt{5}}{15}$$

$$2x \ 3y \ m \ 0 \quad (3,2) \quad m \ 12$$

$$l \quad 2x \ 3y \ 12 \ 0$$

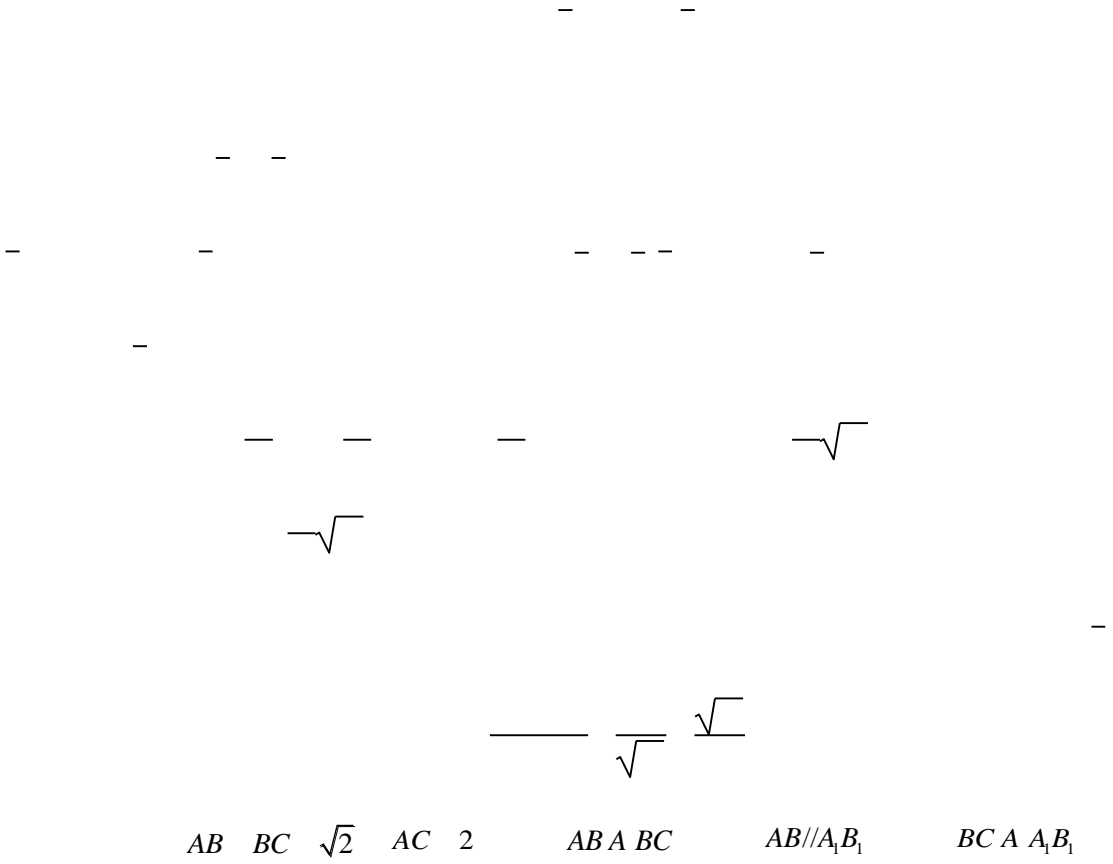
$$y \ kx \quad (3,2) \quad k \ \frac{2}{3} \quad 2x \ 3y \ 0$$

$$\frac{x}{a} \ \frac{y}{b} \ 1 \quad \frac{3}{a} \ \frac{2}{b} \ 1 \quad a \ 9, b \ 3$$

$$x \ 3y \ 9 \ 0 \quad 2x \ 3y \ 0 \quad x \ 3y \ 9 \ 0$$

$$l \quad \frac{x}{a} \ \frac{y}{b} \ 1 \quad (3,2) \quad \frac{3}{a} \ \frac{2}{b} \ 1 \quad t \ 2 \sqrt{\frac{2}{a} \frac{2}{b}} \quad abt \ 24$$

$$\frac{3}{a} \ \frac{3}{b} \ \frac{1}{2} \quad 'ABO \quad 2x \ 3y \ 12 \ 0$$



A_1

$$\because BC \perp CD \quad N \in BD \quad NC = \frac{1}{2}BD = \frac{\sqrt{2}}{2}$$

$$M \in AD \quad MN = \frac{1}{2}AB = \frac{\sqrt{2}}{2} \quad MN \parallel AB$$

$$\because MC = 1 \quad MN^2 + NC^2 = MC^2 \quad MN \perp NC$$

$$\because AB \perp BD \quad MN \perp NC \quad \therefore BD \cap NC = N \quad MN \perp BCD$$

$$\because MN \perp MNC \quad MNC \perp A \quad BCD$$

$$\because MN \perp A \quad BCD \quad AB \parallel MN \quad AB \perp BCD \quad \therefore BC \perp BCD$$

$AB \perp BC$

$$\because AB \perp BD \quad D \in BA \quad C \quad \angle CBD = 60^\circ$$

$$BC = BD \cos 60^\circ = \frac{\sqrt{2}}{2} \quad CD = BD \sin 60^\circ = \frac{\sqrt{6}}{2}$$

$$B \quad BC = BA \quad x = y$$

$$B(0,0,0)$$

$$C \left(\frac{\sqrt{2}}{2}, 0, 0 \right) \quad A(0, \sqrt{2}, 0) \quad D \left(\frac{\sqrt{2}}{2}, 0, \frac{\sqrt{6}}{2} \right) \quad M \left(\frac{\sqrt{2}}{4}, \frac{\sqrt{2}}{2}, \frac{\sqrt{6}}{4} \right) \quad N \left(\frac{\sqrt{2}}{4}, 0, \frac{\sqrt{6}}{4} \right)$$

$$MNC \quad \vec{n} = (x, y, z) \quad \vec{NM} = \left(0, \frac{\sqrt{2}}{2}, 0 \right) \quad \vec{CN} = \left(\frac{\sqrt{2}}{4}, 0, \frac{\sqrt{6}}{4} \right)$$

$$\begin{cases} \vec{n} \cdot \vec{NM} = \frac{\sqrt{2}}{2}y = 0 \\ \vec{n} \cdot \vec{CN} = \frac{\sqrt{2}}{4}x + \frac{\sqrt{6}}{4}z = 0 \end{cases} \quad x = \sqrt{3}z \quad \vec{n} = (\sqrt{3}, 0, 1)$$

$$\vec{BM} = \left(\frac{\sqrt{2}}{4}, \frac{\sqrt{2}}{2}, \frac{\sqrt{6}}{4} \right) \quad \cos \langle \vec{BM}, \vec{n} \rangle = \frac{|\vec{BM} \cdot \vec{n}|}{|\vec{BM}| |\vec{n}|} = \frac{\frac{\sqrt{6}}{2}}{\frac{\sqrt{6}}{2} \cdot 2} = \frac{\sqrt{6}}{4}$$

$$BM \perp MNC \quad \frac{\sqrt{6}}{4}$$

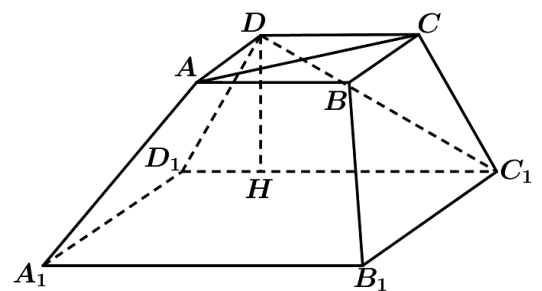
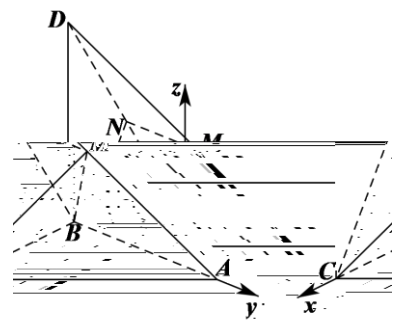
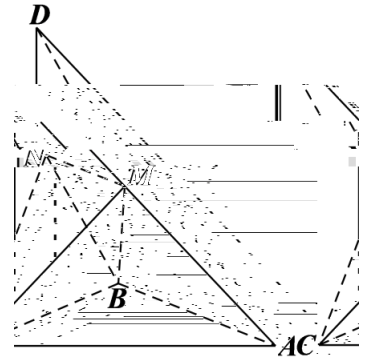
$CC_1 D_1 D$

$$CC_1 \perp CD \quad DD_1 \perp \frac{1}{2}C_1 D_1 \quad \perp$$

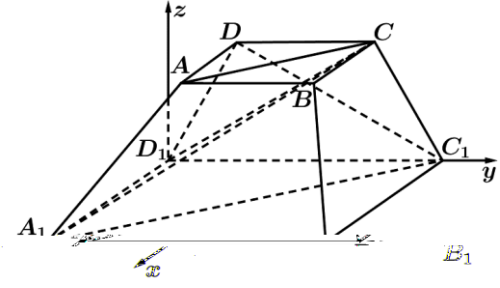
$$DH \perp DC_1 \quad H \in D_1 C_1 \quad D_1 H = \frac{1}{2} \quad \cos \angle DD_1 H = \frac{1}{2} \quad \angle DD_1 C_1 = \frac{\pi}{3}$$

$$DC_1 \perp DD_1 \quad DC_1 = \sqrt{3} \quad DC_1^2 + DD_1^2 = D_1 C_1^2 \quad DC_1 \perp DD_1$$

$$AA_1 D_1 D \perp CC_1 D_1 D \quad DD_1 \perp DC_1 \perp AA_1 D_1 D$$



$AD \cdot AA_1D_1D \quad ADA DC_1 \quad ADA DC \quad DC \cap DC_1 \quad D$
 $ADA \quad CC_1D_1D$
 $A_1C_1 \quad A_1D_1A \quad CC_1D_1D$
 D_1
 $A_1D_1A \quad CC_1D_1D \quad A_1C \quad CC_1D_1D \quad D_1C$
 $A_1C \quad CC_1D_1D \quad A_1CD_1 \quad A_1CD_1 \quad \frac{S}{3}$
 $Rt\triangle A_1CD_1 \quad CD_1 \quad \sqrt{3} \quad A_1D_1 \quad 3$



$$D_1 \quad 0,0,0 \quad A_1 \quad 3,0,0 \quad D \quad 0, \frac{1}{2}, \frac{\sqrt{38}}{2} \quad C \quad 0, \frac{3}{2}, \frac{\sqrt{38}}{2} \quad C_1 \quad 0,2,0$$

$$\overline{D_1D} \quad 0, \frac{1}{2}, \frac{\sqrt{38}}{2} \quad \overline{D_1A_1} \quad 3,0,0 \quad \overline{A_1C_1} \quad 3,2,0 \quad \overline{A_1C} \quad 3, \frac{3}{2}, \frac{\sqrt{38}}{2}$$

$$AA_1D_1D \quad \vec{m} \quad x, y, z \quad \begin{matrix} \circ \vec{m} \cdot \overline{D_1D} \sim 0 \\ \textcircled{R} \vec{m} \cdot \overline{D_1A_1} \sim 0 \end{matrix} \quad \begin{matrix} \circ \frac{1}{2}y + \frac{\sqrt{38}}{2}z = 0 \\ \textcircled{R} 2y + \sqrt{38}z = 0 \\ \circ 3x = 0 \end{matrix}$$

$$y = 3 \quad x = 0 \quad z = \sqrt{3} \quad \vec{m} = 0, 3, \sqrt{3}$$

$$AA_1C_1C \quad \vec{n} \quad a, b, c \quad \begin{matrix} \circ \vec{n} \cdot \overline{A_1C_1} \sim 0 \\ \textcircled{R} \vec{n} \cdot \overline{A_1C} \sim 0 \end{matrix} \quad \begin{matrix} \circ 3a - 2b = 0 \\ \textcircled{R} 3a - \frac{3}{2}b - \frac{\sqrt{3}}{2}c = 0 \\ \circ 3a - \frac{3}{2}b - \frac{\sqrt{3}}{2}c = 0 \end{matrix}$$

$$a = 2 \quad b = 3 \quad c = \sqrt{3} \quad \vec{n} = 2, 3, \sqrt{3} \quad |\cos \langle \vec{m}, \vec{n} \rangle| = \frac{|\vec{m} \cdot \vec{n}|}{|\vec{m}| |\vec{n}|} = \frac{6}{2\sqrt{3} \cdot 4} = \frac{\sqrt{3}}{4}$$

$$C \quad AA_1 \quad D \quad C \quad AA_1 \quad D \quad \frac{\sqrt{3}}{4}$$

