

$$A = \{x|x^2 - 2x - 3 < 0\} \quad B = \{x|2^{x+1} > 1\} \quad \complement_B A = ( \quad )$$

$$[3, +\infty) \quad (3, +\infty) \quad (-\infty, -1] \cup [3, +\infty) \quad (-\infty, -1) \cup (3, +\infty)$$

$$(1 + \frac{1}{x^2})(1+x)^6 \quad x^2$$

$$( \quad ) \quad - \quad \sqrt{\quad} \quad -$$

$a \quad b \quad c$

$$R \quad f(x) \quad \underline{\underline{f(x+2) = -\frac{1}{f(x)}}} \quad (0, 1) \quad f(x) = 3^x \quad f(\log_3 54) = ( \quad )$$

$$\frac{3}{2} \quad \frac{2}{3} \quad \frac{3}{2} \quad \frac{2}{3}$$

$$f(x) \quad \underline{\underline{(-\infty, +\infty)}} \quad f(1) = -1$$

$$-1 \leq f(x-2) \leq 1 \quad x \quad ( \quad )$$

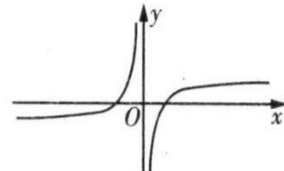
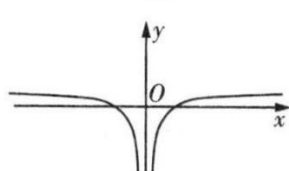
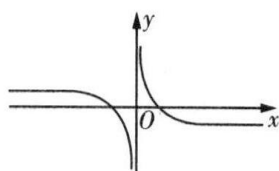
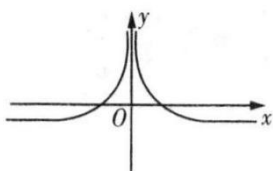
$$[-2, 2] \quad [-1, 1] \quad [0, 4] \quad [1, 3]$$

$$x \quad y \quad \left\{ \quad \quad \quad \right. \quad \text{---} \quad ( \quad )$$

$$(-\infty, -8] \cup [1, +\infty) \quad (-\infty, -10] \cup [-1, +\infty)$$

$$( \quad )$$

$$f(x) = \begin{cases} \frac{\ln x}{1+x}, x > 0 \\ \frac{\ln(-x)}{1-x}, x < 0 \end{cases} \quad ( \quad )$$



$a \quad b$

$$\text{---} \quad \text{---} \quad ( \quad )$$

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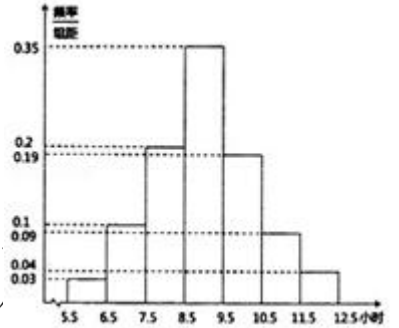
$X( )$

(1)  $\bar{x} \quad s^2( )$

(2)  $N(\mu, \sigma^2)$

(i)

$X \sim N(\mu, \sigma^2) \quad Y = \frac{X - \mu}{\sigma} \quad Y \sim N(0, 1) \quad P(X \leq a) = P\left(Y \leq \frac{a - \mu}{\sigma}\right)$   
 $P(X \leq 10)$



(ii)

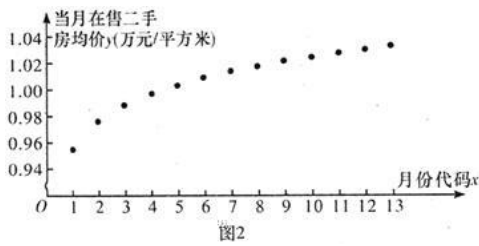
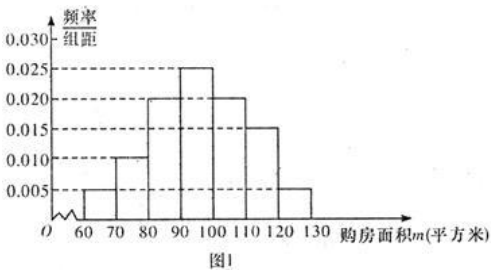
$P(Z \geq 2) (0.0001) \quad \sqrt{178} \approx \frac{40}{3}, 0.7734^{19} \approx 0.0076.$

$Y \sim N(0, 1) \quad P(Y \leq 0.75) = 0.7734$

$60 \leq m \leq 130$   $m($

$y( / ) ($

$1 - 13 )$



(1)  $\bar{m} ( )$

(2)

(3)  $\hat{y} = \hat{a} + \hat{b}\sqrt{x} \quad \hat{y} = \hat{c} + \hat{d} \ln x$

$\hat{y} = 0.9554 + 0.0306 \ln x$

	<del>0.005459</del>	$\hat{y} = 0.9554 + 0.0306 \ln x$
$\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})$	0.005459	0.005886
$\sqrt{\sum_{i=1}^n (x_i - \bar{x})^2 \sum_{i=1}^n (y_i - \bar{y})^2}$	0.006050	

( 0.001)

$\ln 2 \approx 0.69, \ln 3 \approx 1.10, \ln 15 \approx 2.71, \sqrt{3} \approx 1.73, \sqrt{15} \approx 3.87, \sqrt{17} \approx 4.12$

$$r = \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_{i=1}^n (x_i - \bar{x})^2 \sum_{i=1}^n (y_i - \bar{y})^2}}$$

$$f(x) = \log_{\frac{1}{2}}(x^2 + 1) \quad g(x) = x^2 - ax + 6$$

(1)  $g(x)$

$g(x)$

(2)  $g(x) < 0 \quad \{x | 2 < x < 3\} \quad x > 1 \quad \frac{g(x)}{x-1}$

(3)  $x_1 \in [1, +\infty), x_2 \in [-2, 4] \quad f(x_1) \leq g(x_2)$

$$f(x) = a - \frac{1}{2^x + 1}$$

(1)

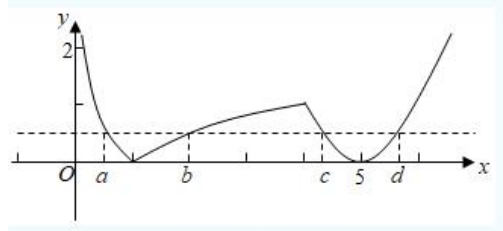
(2)  $f(x)$  ( )  $f(x)$

(3)

ACACD ACCCB BD ABD

$$(4, +\infty) \quad -x(1-x) \quad \frac{13}{28} \quad (24, 25) \quad \left(-\infty, -\frac{2}{e}\right]$$

$$f(x) = \begin{cases} |\log_4 x|, & 0 < x \leq 4 \\ x^2 - 10x + 25, & x > 4 \end{cases}$$



$$\therefore a < b < c < d \quad a < b < c < d \quad f(a) = f(b) = f(c) = f(d)$$

$$-\log_4 a = \log_4 b \quad \log_4 a + \log_4 b = 0 \quad ab = 1$$

$$abcd = cd$$

$$c + d = 10 \quad cd < \left(\frac{c+d}{2}\right)^2 = 25$$

$$cd = c(10-c) = -(c-5)^2 + 25 \quad c \in (4, 5)$$

$$\therefore cd > 24$$

$$abcd \quad (24, 25)$$

$$(24, 25)$$

$$a \leq x \ln x + ex^2 - 2x$$

$$f(x) = x \ln x \quad g(x) = ex^2 - 2x$$

$$h(x) = f(x) + g(x) \quad a \leq h(x)_{\min}$$

$$g(x) = e\left(x - \frac{1}{e}\right)^2 - \frac{1}{e}$$

$$f'(x) = \ln x + 1 \quad 0 < x < \frac{1}{e} \quad f'(x) < 0 \quad x > \frac{1}{e} \quad f'(x) > 0$$

$$x = \frac{1}{e} \quad f(x) \quad g(x)$$

$$h(x)_{\min} = h\left(\frac{1}{e}\right) = -\frac{2}{e}$$

∴ ?

$$\left(-\infty, -\frac{2}{e}\right]$$

$$(1) \bar{x} = 6 \times 0.03 + 7 \times 0.1 + 8 \times 0.2 + 9 \times 0.35 + 10 \times 0.19 + 11 \times 0.09 + 12 \times 0.04 = 9$$

$$s^2 = (6-9)^2 \times 0.03 + (7-9)^2 \times 0.1 + (8-9)^2 \times 0.2 + (9-9)^2 \times 0.35 \\ + (10-9)^2 \times 0.19 + (11-9)^2 \times 0.09 + (12-9)^2 \times 0.04 = 1.78$$

$$(2)(i) \quad \mu = 9 \quad \sigma^2 = 1.78 \quad \therefore X \sim N(9, 1.78) \quad \sigma = \sqrt{1.78} = \frac{\sqrt{178}}{10} \approx \frac{4}{3}$$

$$P(X \leq 10) = P\left(\frac{X-9}{\frac{4}{3}} \leq \frac{10-9}{\frac{4}{3}}\right) = P\left(Z \leq \frac{3}{4}\right) = 0.7734$$

$$(ii) (i) \quad P(X > 10) = 1 - P(X \leq 10) = 0.2266$$

$$Z \sim B(20, 0.2266)$$

$$P(Z \geq 2) = 1 - P(Z = 0) - P(Z = 1) = 1 - 0.7734^{20} - C_{20}^1 \times 0.2266 \times 0.7734^{19} \\ = 1 - (0.7734 + 20 \times 0.2266) \times 0.0076 \approx 0.9597$$

$$\therefore Z \quad E(Z) = 20 \times 0.2266 = 4.532$$

$$(1) \bar{m} = 65 \times 0.05 + 75 \times 0.1 + 85 \times 0.2 + 95 \times 0.25 + 105 \times 0.2 + 115 \times 0.15 + 125 \times 0.05 = 96$$

$$(2) \quad 0.20 + 0.15 + 0.05 = 0.4$$

$$\therefore X \sim B(3, 0.4)$$

$$\therefore P(X = k) = C_3^k \times 0.4^k \times 0.6^{3-k} (k = 0, 1, 2, 3)$$

$\therefore$

$X$				
$P(X)$	0.216	0.432	0.288	0.064

$$\therefore E(X) = 0.432 + 0.288 \times 2 + 0.064 \times 3 = 1.2$$

$$(3) \quad r_1, r_2$$

$$r_1 = 1 - \frac{0.000591}{0.00605}, r_2 = 1 - \frac{0.000164}{0.00605}, \therefore r_1 < r_2$$

$$x = 15$$

$$0.00591 + 0.000164 = 0.006074 \approx 0.00605$$

$$(1) \because g(x) \quad \therefore a(-x) = a(x)$$

$$(-x)^2 + ax + 6 = x^2 - ax + 6 \quad ax = 0 \quad x \in R \quad \therefore a = 0$$

$$\therefore g(x) = x^2 + 6$$

$$\therefore g(x) \quad x = 0$$

$$\therefore g(x) \quad (0, +\infty)$$

$$(2) \because g(x) = x^2 - ax + 6 < 0 \quad \{x | 2 < x < 3\}$$

$$\therefore 2 \quad x^2 - ax + 6 = 0$$

$$a = 2 + 3 = 5$$

$$\therefore g(x) = x^2 - 5x + 6$$

$$\therefore \frac{g(x)}{x-1} = \frac{x^2 - 5x + 6}{x-1} = (x-1) + \frac{2}{x-1} - 3$$

$$\because x > 1 \quad \therefore x-1 > 0$$

$$(x-1) + \frac{2}{x-1} \geq 2\sqrt{2} \quad \begin{cases} x-1 = \frac{2}{x-1} \\ x-1 > 0 \end{cases} \quad x = \sqrt{2} + 1 =$$

$$\therefore \frac{g(x)}{x-1} \geq 2\sqrt{2} - 3 \quad \frac{g(x)}{x-1} \geq 2\sqrt{2} - 3 \quad x = \sqrt{2} + 1 =$$

$$(3) \because x \geq 1 \quad f(x) = \log_2(x^2 + 1) \leq -1, \quad x = 1 \quad f(x) \quad f(1) = -1$$

$$\because \quad \underline{x_1 \in [1, +\infty), x_2 \in [-2, 4]} \quad f(x_1) \leq g(x_2)$$

$$\therefore \quad [-2, 4] \quad g(x) \geq f(x)_{\max} \quad x^2 - ax + 6 \geq -1 \quad x \in [-2, 4]$$

$$\frac{F(x)}{x-1} \geq \frac{2}{x-1} - 3 \quad x \in [-2, 4]$$

$$\textcircled{1} \quad a \leq -4 \quad F(x)_{\min} = F(-2) = 2a + 11$$

$$\frac{11}{2} \geq 0 \Rightarrow a \geq -\frac{11}{2}$$

$$\therefore -\frac{11}{2} \leq a \leq -4;$$

$$-4 < a < 8 \quad \frac{F(x)}{4} \geq \frac{F(a)}{2} = \frac{a^2 + 7}{2}$$

$$-\frac{a^2}{4} + 7 \geq 0 \Rightarrow -2\sqrt{7} \leq a \leq 2\sqrt{7}$$

$$\therefore A \leq a \leq 2\sqrt{7}$$

$$\textcircled{3} \quad a \geq 8 \quad F(x)_{\min} = F(4) = -4a + 23$$

$$-4a + 23 \geq 0 \Rightarrow a \leq \frac{23}{4}$$

$$\therefore a \in \emptyset$$

$$a \quad -\frac{11}{2} \leq a \leq 2\sqrt{7}$$

$$\frac{f(x)}{2^x+1} = \frac{1}{2^x} \quad R$$

$$\therefore f(0) = 0 \quad a = \frac{1}{2}$$

$$f(x) = \frac{1}{2} - \frac{1}{2^x+1} = \frac{1}{2} \cdot \frac{2^x-1}{2^x+1}$$

$$f(-x) = -f(x)$$

$$\therefore a = \frac{1}{2}$$

$$(2) f(x) \quad R$$

$$\because 2^x + 1 > 1 \quad \therefore 0 < \frac{1}{2^x+1} < 1$$

$$-\frac{1}{2} < \frac{1}{2} - \frac{1}{2^x+1} < \frac{1}{2}$$

$$\therefore f(x) \in \left(-\frac{1}{2}, \frac{1}{2}\right)$$

$$(3)$$

$$f[(\log_2 x)^2 - b] = f(\log_2 x) \quad \left[\frac{1}{2}, 2\right]$$

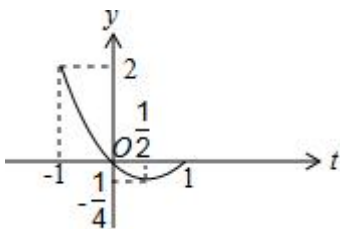
$$(2) \quad f(x) \quad R$$

$$\therefore (\log_2 x)^2 - b = \log_2 x \quad b = (\log_2 x)^2 - \log_2 x \quad \left[\frac{1}{2}, 2\right]$$

$$\log_2 x = t \quad \because x \in \left[\frac{1}{2}, 2\right] \quad \therefore t \in [-1, 1]$$

$$b = t^2 - t \quad t \in [-1, 1]$$

$$y = t^2 - t$$



$$b \in \left(-\frac{1}{4}, 0\right]$$

$$y = t^2 - t \quad y = b$$

$$b = t^2 - t$$

$$\therefore b \in \left(-\frac{1}{4}, 0\right]$$